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$Cu(Cu_{0.44}Cr_{4.56})Ge_2O_{12}$: a closepacked oxide with CuO_4 tetrahedra

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The structure of copper(I,II) pentachromium(III) germanate, Cu(Cu_{0.44}Cr_{4.56})Ge₂O₁₂, contains one Cu position (*m*2*m*), one Ge position (*m*) and three Cr positions (2/*m*, *m* and 2). The close-packed structure is described in terms of slabs of edgesharing $Cr^{3+}O_6$ octahedra and isolated CuO₄ and GeO₄ tetrahedra. These slabs are aligned parallel to the *bc* plane and are separated from each other by GeO₄ tetrahedra along *a*. The tetrahedral coordination observed for the Cu⁺/Cu²⁺ ions represents an unusual feature of the structure. The Cr-Oand Cu-O bond lengths are compared with literature data.

Comment

Cu(Cu_{0.44}Cr_{4.56})Ge₂O₁₂ was synthesized during our investigation of Cu-containing germanates (Redhammer & Roth, 2004*a*; Redhammer *et al.*, 2005). It represents a new structure type and, to the best of our knowledge, is the first copper chromium germanate reported. Lambert & Eysel (1968) were the only workers to study the CuO–Cr₂O₃–GeO₂ system previously and they noted the absence of ternary compounds. It may also be noted that Cr-containing germanates are also rare, with only seven entries in the current Inorganic Crystal Structure Database (ICSD, 2006), including cubic and tetragonal spinels (Hirota *et al.*, 1990; Isasi *et al.*, 1996) and pyroxene-type LiCrGe₂O₆ (Redhammer & Roth, 2004*b*). In contrast, a larger number of copper germanates are known.

The asymmetric unit of the title crystal structure contains one Cu-, three Cr-, one Ge- and five O-atom positions (Fig. 1). The structure is built of edge-sharing CrO_6 octahedra that also share corners with CuO_4 and GeO_4 tetrahedra (Figs. 2 and 3). The basic unit of the structure is a (100) slab containing the Cu tetrahedra and Cr1–Cr3 octahedra, with adjacent slabs being linked to each other along *a* by the GeO₄ tetrahedra. An alternative description of the structure emphasizes the cubic close-packed arrangement of the O atoms (Fig. 3) and reveals a topology closely related to the spinel structure type and the orthorhombic $M_3(VO_4)_2$ structure type (Sauerbrei *et al.*, 1973). Indeed, the structure of the title compound can be described as a 1:1 intergrowth of spinel and $M_3(VO_4)_2$ slabs along the *a* axis (*i.e.* $M_2TO_4 + M_3T_2O_8 = M_5T_3O_{12}$, where *M* are octahedrally and *T* are tetrahedrally coordinated cations).

The bond lengths, the O–O edge lengths and the volume of the $Cr1O_6$ octahedron are all distinctly different from those of the $Cr2O_6$ and $Cr3O_6$ octahedra (Tables 1 and 2). The Cr1-O bond lengths vary between 1.941 (3) and 2.111 (2) Å, and this upper value is large for Cr^{3+} –O bonds, as shown by an





A view of the asymmetric unit and some symmetry-related atoms of the title compound, showing 95% probability displacement ellipsoids and the atom-numbering scheme. [Symmetry codes: (i) $x, y, \frac{3}{2} - z$; (ii) x, -y, 1 - z; (iii) $1 - x, -y, \frac{1}{2} + z$; (iv) $1 - x, y, \frac{3}{2} - z$; (v) x, 1 - y, 1 - z; (vi) $1 - x, 1 - y, -\frac{1}{2} + z$; (vii) $1 - x, y, \frac{1}{2} - z$; (viii) $x, y, \frac{1}{2} - z$; (ix) $\frac{1}{2} - x, -\frac{1}{2} + z$; (x) $x, -y, -\frac{1}{2} + z$; (x) $\frac{1}{2} - x, -\frac{1}{2} + y, \frac{1}{2} - z$; (xii) x, -y, -z.]



Figure 2

A view of the structure of the title compound along the c direction, showing the Cr1–Cr3 octahedra, the Ge sites (small spheres) and the Cu1 sites (large spheres).

evaluation of 925 individual bonds in 130 compounds in the ICSD that yielded a mean Cr–O value of 1.982 Å (σ = 0.089 Å), with only a few bonds longer than 2.10 Å (Fig. 4a). The large mean Cr1-O bond length, the low bond-valence sum [S = 2.52 valence units (v.u.); Brese & O'Keeffe, 1991] and the overpopulation of the Cr1 site when solely filled with Cr (see below) are all evidence for a mixed (Cr+Cu) occupancy of this site. Assuming valences of +3 and +2 for Cr and Cu, respectively, the refined content of Cr_{0.56}Cu_{0.44} yields a nominal valence of 2.56 v.u., in good agreement with the bondvalence sum S = 2.52 v.u. While the bond-length distortion (BLD; Renner & Lehmann, 1986) is large for the Cr1O₆ octahedron, the octahedral angle variance (OAV) and the quadratic octahedral elongation (QOE) (Robinson et al., 1971) are the lowest of all three CrO_6 octahedra (Table 2). The Cr1 site is thus regular in terms of the angular distortion, but shows a distinct tetragonal compression along the b axis.

The Cr2 site shows a more regular BLD, with typical Cr2– O bond lengths (Table 2 and Fig. 4*a*). Similar to Cr1, the Cr2 site is characterized by a high fraction of shared O–O edges. As a result, the Cr···Cr distances are shorter than 3.00 Å (Table 2). The Cr3O₆ octahedron has the smallest number of shared edges, with the most regular BLD and the largest angular distortion and quadratic elongation (Table 2).

The most unusual feature of the structure is the tetrahedral coordination of the Cu1 site with m2m symmetry. Given the Cu²⁺ and Cr³⁺ mixing on the Cr1 site, it follows that the Cu1 site must be occupied by Cu⁺ and Cu²⁺ for charge balance. This is also supported by the bond-valence sum, which is significantly higher than 1 v.u. (Table 2). The Cu1O₄ tetrahedron is almost ideal, with small distortion parameters (Table 2) and nearly ideal bond angles (Table 1). Interestingly, it is more regular than the GeO₄ tetrahedron.

Copper is not frequently found in a tetrahedral coordination. An evaluation of 170 compounds in the ICSD containing 600 individual Cu^+-O bonds showed the following distribu-



Figure 3

A view of the structure of the title compound along the a direction.

tion of coordination environments: threefold (\sim 5%), sixfold $(\sim 5\%)$ and fourfold $(\sim 18\%)$, with the remaining $\sim 72\%$ in twofold coordination. Among the four-coordinated Cu⁺ ions, approximately one third are in a square-planar environment and two thirds in a tetrahedral environment. The individual Cu^+ -O bond lengths are scattered between 1.70 and 2.30 Å (Fig. 4b), with a distribution strongly influenced by the coordination geometry. For twofold coordination, the majority of data lie between 1.80 and 1.93 Å (average value = 1.867 Å, σ = (0.072) (inset in Fig. 4b). For square-planar coordination, one finds a rather narrow distribution with an average bond length of 1.946 Å ($\sigma = 0.052$). For tetrahedral coordination, the bond lengths are between 1.83 and 2.28 Å (average value = 2.045 Å, $\sigma = 0.094$). The Cu1–O bonds in the title compound match the average tetrahedral Cu⁺-O bond length very well. In most compounds containing Cu⁺O₄ tetrahedra, these are strongly distorted (flattened) and only spinels, such as Cu_{1.5}Mn_{1.5}O₄ and CuMg_{0.5}Mn_{1.5}O₄ (Vandenberghe et al., 1976) or CuFe₅O₈ (Mexmain, 1971), contain regular tetrahedra. This again illustrates the relationship between the spinel structure type and the title compound.

As in the case of Cu^+ , tetrahedral coordination for Cu^{2+} is rare, due to the specific electronic configuration of the cation



Figure 4

Histogram plots of (a) 925 individual Cr^{3+} —O bond lengths and (b) 600 Cu^+ —O bond lengths, taken from the ICSD. The histogram groups have a width of 0.005 Å. [2] and [4] superscripts in the inset denote two- and fourfold oxygen coordination, respectively.

4822 measured reflections

 $R_{\rm int}=0.042$

 $\theta_{\rm max} = 28.8^{\circ}$

595 independent reflections

481 reflections with $I > 2\sigma(I)$

(Jahn-Teller distortion). Only a few examples are known, such as akermanite-type Ba₂CuGe₂O₇ (Tovar et al., 1998), spineltype CuCr₂O₄ and CuRh₂O₄ (Dollase & O'Neill, 1997), or pollucite-type Cs₂CuSi₅O₁₂ (Heinrich & Baerlocher, 1991). The Cu²⁺O₄ tetrahedra are distinctly flattened in all these structures. Thus, the almost ideal tetrahedral coordination of Cu in the title compound can indeed be regarded as a rather unusual feature of the structure. However, it should be noted that the atomic displacement of Cu1 is rather large, a fact that might indicate split sites for Cu1 (see *Refinement* section).

Although the GeO_4 tetrahedron, with site symmetry *m*, is more distorted than the CuO₄ tetrahedron (Table 2), it is still rather regular. By comparison, the GeO₄ tetrahedra in Ca_{7.96}Cu_{0.04}Ge₅O₁₈ (Redhammer et al., 2006), CaZn₂Ge₂O₇ (Redhammer & Roth, 2006), CaCuGe₂O₆ (Redhammer et al., 2005) or $Cu_2Sc_2Ge_4O_{13}$ (Redhammer & Roth, 2004*a*) all exhibit larger polyhedral distortions, especially in terms of the tetrahedral angle variance and quadratic tetrahedral elongation. The longest Ge–O bond in the title compound is Ge– O1, which is 0.02 Å longer than Ge-O2 or Ge-O3 (Table 2). Atom O1 is bonded to one Ge and three Cr atoms, while atoms O2 and O3 are bonded to one Ge and two Cr atoms only. With four bonds contributing to the bond-valence sum of O1, individual bonds to O1 are expected to be weaker, and hence longer. Stronger repulsions between Ge⁴⁺ and the three neighbouring Cr³⁺ ions around O1 may also be responsible for the longer Ge-O1 bond.

Experimental

The title compound was found by chance in an attempt to grow crystals of Cu₂Cr₂Ge₄O₁₃, an analogue of Cu₂Sc₂Ge₄O₁₃ (Redhammer et al., 2005), by slow cooling from the melt. For this purpose, a stoichiometric homogenous mixture of CuO, Cr2O3 and GeO₂ was carefully ground in an agate mortar and placed in a small open platinum tube (length 30 mm, internal diameter 5 mm). This assemblage was transferred to a high-temperature furnace, slowly heated to 1773 K at a rate of 1 K min⁻¹, held at this temperature for 12 h to homogenize the melt and cooled to 1323 K at a rate of 0.03 K min⁻¹. The products consisted mainly of CuGeO₃, GeO₂, minor Cr₂GeO₅ and some very small prismatic to needle-like black crystals of the title compound (less than 5% by volume). Semiquantitative energy-dispersive X-ray (EDX) analysis showed that only Cu, Cr, Ge and O were present. The average composition from ten analyses of three different crystals was (in atom% and normalized to 100): 7.47 (9) Cu, 22.20 (11) Cr, 9.97 (7) Ge and 60.36 (21) O, yielding a formula of Cu_{1.48}Cr_{4.41}Ge_{1.98}O₁₂. Due to the small size of the crystals, we were unable to perform an electron microprobe analysis. According to Breuer et al. (1986), the reduction of CuO to Cu₂O takes place at 1293 K in air. The presence of Cu⁺ in the title compound is therefore not unexpected based on the synthesis conditions.

Crystal data

$Cu(Cu_{0.44}Cr_{4.56})Ge_2O_{12}$	Z = 4
$M_r = 665.78$	$D_x = 5.305 \text{ Mg m}^{-3}$
Orthorhombic, Cmcm	Mo $K\alpha$ radiation
a = 17.176 (2) Å	$\mu = 16.49 \text{ mm}^{-1}$
b = 8.2272 (10) Å	T = 295 (2) K
c = 5.8996 (7) Å	Needle, black
$V = 833.68 (17) \text{ Å}^3$	$0.09 \times 0.03 \times 0.03$ mm

Bruker	SMART	APEX

diffractometer Rotation, ω scans at four different φ positions Absorption correction: numerical via equivalents using X-SHAPE

(Stoe & Cie, 1996) $T_{\min} = 0.55, \ T_{\max} = 0.61$

Refinement

Refinement on F^2	$w = 1/[\sigma^2(F_o^2) + (0.0261P)^2]$
$R[F^2 > 2\sigma(F^2)] = 0.024$	where $P = (F_o^2 + 2F_c^2)/3$
$wR(F^2) = 0.053$	$(\Delta/\sigma)_{\rm max} < 0.001$
S = 1.04	$\Delta \rho_{\rm max} = 0.90 \ {\rm e} \ {\rm \AA}^{-3}$
595 reflections	$\Delta \rho_{\rm min} = -0.71 \text{ e } \text{\AA}^{-3}$
62 parameters	

Table 1

Selected geometric parameters (Å, °).

Cu1 $-$ O4 Cu1 $-$ O5 ⁱ Ge $-$ O2 Ge $-$ O3 Ge $-$ O1 Cr1 $-$ O4 Cr1 $-$ O1 Cr1 $-$ Cr1 ⁱⁱ Cr2 $-$ Cr2 ⁱⁱⁱ Cr2 $-$ Cr2 ⁱⁱⁱⁱ	2.026 (3) 2.038 (3) 1.755 (2) 1.757 (3) 1.778 (4) 1.941 (3) 2.111 (2) 2.9498 (4) 2.9498 (4)	$\begin{array}{c} Cr1 - Cr2 \\ Cr2 - Cr3 \\ Cr2 - O5 \\ Cr2 - O4 \\ Cr2 - O1^{iv} \\ Cr2 - O2 \\ Cr3 - O5 \\ Cr3 - O2^{v} \end{array}$	2.9004 (7) 2.9587 (7) 1.939 (4) 1.965 (2) 2.002 (4) 2.004 (2) 1.974 (2) 1.985 (2)
$04^{vi} - Cu1 - 04$ $04^{vi} - Cu1 - 05^{i}$ $05^{i} - Cu1 - 05^{vii}$ $02 - Ge - 02^{vi}$	110.36 (19) 109.59 (7) 108.1 (2) 109.64 (15)	02-Ge-O3 02-Ge-O1 03-Ge-O1	111.72 (9) 109.10 (10) 105.44 (17)

Symmetry codes: (i) x, -y, -z + 1; (ii) $-x + 1, -y + 1, z + \frac{1}{2}$; (iii) $x, y, -z - \frac{1}{2}$; (iv) x, -y + 1, -z + 1; (v) $x, -y, z - \frac{1}{2};$ (vi) $x, y, -z + \frac{3}{2};$ (vii) -x + 1, -y, -z + 1.

Table 2

Selected structural and polyhedral distortion parameters for the title compound.

	Ge	Cu1	
< <i>T</i> -O> (Å)	1.762	2.032	
<o-o>(Å)</o-o>	2.876	3.318	
BLD† (%)	0.41	0.30	
Volume ($Å^3$)	2.800	4.31	
TAV‡ (°)	5.323	0.55	
TQE§	1.0013	1.0001	
<i>S</i> ¶ (v.u.)	3.86	1.28	
	Cr1	Cr2	Cr3
<cr-o> (Å)</cr-o>	2.055	1.980	1.980
<o-o> (Å)</o-o>	2.906	2.780	2.797
BLD† (%)	3.68	1.18	0.21
Volume (Å ³)	11.47	10.22	10.20
$OAV^{\dagger\dagger}(^{\circ})$	12.84	29.47	34.16
OQE‡‡	1.0068	1.0085	1.0096
<i>S</i> ¶ (v.u.)	2.52	3.01	3.00

† Bond-length distortion, BLD = $(100/n) \sum_{i=1}^{n} [\{(X-O)_i - (\langle X-O \rangle)\}/(\langle X-O \rangle)],$ where n = number of bonds, $(X - O)_i =$ central cation-oxygen length and $\langle X - O \rangle =$ average cation-oxygen bond length (Renner & Lehmann, 1986). ‡ Tetrahedral angle variance, TAV = $\sum_{i=1}^{n} (\Theta_i - 109.47)^2 / 5$, with Θ_i = individual O-T-O tetrahedral bonding angle (Robinson *et al.*, 1971). § Tetrahedral quadratic elongation, TQE = $\sum_{i=1}^{4} (l_i/l_1)^2/4$, where l_{t} = centre-to-vertex distance for a regular tetrahedron whose volume is equal to that of the undistorted tetrahedron with bond length l_i (Robinson *et al.*, 1971). ¶ Bondvalence sum S (Brese & O'Keeffe, 1991). †† Octahedral angle variance, OAV = $\sum_{i=1}^{n} (\Theta_i - 90)^2 / 11$ (Robinson *et al.*, 1971). \ddagger Octahedral quadratic elongation, OQE = $\sum_{i=1}^{6} (l_i/l_o)^2/6$, where $l_o =$ centre to vertex distance for a regular octahedron whose volume is equal to that of the undistorted octahedron with bond length l_i (Robinson *et al.*, 1971).

Structure solution using Patterson methods yielded the Cu, Cr and Ge positions, and the O atoms were located from residual electrondensity analysis in subsequent refinement cycles. Full anisotropic refinement on F^2 using fixed site occupancies for the metal sites led to a final wR_2 value of 9.3% and a formula of Cu⁺Cr₅³⁺Ge₂O₁₂. Releasing the site occupancies of all metal sites resulted in a drastic drop of wR_2 to 5.4%, with occupancies of 0.249 (3), 0.499 (3), 0.497 (3) and 0.495 (4) for the Cu, Ge, Cr2 and Cr3 sites, respectively. However, the Cr1 occupancy of 0.279 (3) was significantly above 0.25, indicating that either Ge or Cu also occupied this site. Since the bond-valence sum for Cr1 was significantly below 3.0 and Ge⁴⁺ distinctly prefers tetrahedral coordination, it was concluded that Cu was present on the Cr1 site, at a final occupancy of Cu_{0.44}Cr_{0.56}.

As the displacement parameter for the Cu1 site is almost twice as large as those for the Ge and Cr1–Cr3 sites, the Cu1 occupancy was checked carefully in the final refinement cycles. No reduced occupancy and no substitution by lighter Cr atoms could be detected. The sum formula of $Cu_{1.44}Cr_{4.56}Ge_2O_{12}$ resulting from the structure refinement agrees well with the semi-quantitative energy dispersive X-ray analysis.

The large displacement parameter of the Cu1 site could possibly be the result of positional disorder, which has also been investigated. By fixing U to a value of 0.008 Å² (close to the U values of the other cation sites), the Cu1 site can be split into three subsites, *viz*. Cu1*a* at $4c \left[\frac{1}{2}, 0.124 \ (6), \frac{3}{4}\right]$, Cu1*b* at 8*g* [0.492 (1), 0.138 (2), $\frac{3}{4}$] and Cu1*c* at 8*f* $\left[\frac{1}{2}, 0.112 \ (2), 0.776 \ (7)\right]$, with occupancies of 0.09 (2), 0.07 (2) and 0.08 (3), respectively. Such disorder may reflect the fact that the regular tetrahedral coordination of the unsplit Cu1 site is not ideally suited to either Cu⁺ or Cu²⁺. The Cu1*b* and Cu1*c* positions correspond to distorted tetrahedral coordination environments, with Cu O bond lengths (Å) of 1.97 (1) × 2, 2.00 (1) and 2.21 (1) for Cu1*b*, and of 1.96 (2), 1.99 (2) × 2 and 2.21 (4) for Cu1*c*. The refinement of this split model yields *R* indices similar to those of the unsplit model but is only stable with constrained displacement parameters for Cu1*a*-Cu1*c*.

Data collection: *SMART-Plus* (Bruker, 2001); cell refinement: *SAINT-Plus* (Bruker, 2001); data reduction: *SAINT-Plus*; program(s) used to solve structure: *SHELXS97* (Sheldrick, 1997); program(s) used to refine structure: *SHELXL97* (Sheldrick, 1997); molecular graphics: *DIAMOND* (Brandenburg, 1999); software used to prepare material for publication: *WinGX* (Version 1.70.01; Farrugia, 1999).

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Supplementary data for this paper are available from the IUCr electronic archives (Reference: BC3029). Services for accessing these data are described at the back of the journal.

References

- Brandenburg, K. (1999). *DIAMOND*. Release 2.1c. Crystal Impact GbR, Bonn, Germany.
- Brese, N. E. & O'Keeffe, M. (1991). Acta Cryst. B47, 192-197.
- Breuer, K. H., Eysel, W. & Behruzi, M. (1986). Z. Kristallogr. 176, 219-232.
- Bruker (2001). *SMART-Plus* (Version 5.6) and *SAINT-Plus* (Version 5.0). Bruker AXS Inc., Madison, Wisconsin, USA.
- Dollase, W. A. & O'Neill, H. St C. (1997). Acta Cryst. C53, 657-659.
- Farrugia, L. J. (1999). J. Appl. Cryst. 32, 837-838.
- Heinrich, A. R. & Baerlocher, Ch. (1991). Acta Cryst. C47, 237-241.
- Hirota, K., Inoue, T., Mochida, N. & Ohtsuka, A. (1990). Nippon Seramikkusu Kyokai Gakujutsu Ronbunshi, 98, 976–986.
- ICSD (2006). Inorganic Crystal Structure Database. Version 2006-1. FIZ-Karlsruhe, Germany, and the National Institute of Standards and Technology (NIST), USA. URL: http://www.fiz-karlsruhe.de/ecid/Internet/ en/DB/icsd/.
- Isasi, M. J., Veiga, M. L. & Pico, C. (1996). J. Mater. Sci. Lett. 15, 1022– 1024.
- Lambert, U. & Eysel, W. (1968). Powder Diffr. 1, 45-50.
- Mexmain, J. (1971). Ann. Chim. (Paris), pp. 297-308.
- Redhammer, G. J. & Roth, G. (2004a). J. Solid State Chem. 177, 2714-2725.
- Redhammer, G. J. & Roth, G. (2004b). Z. Kristallogr. 219, 278-294.
- Redhammer, G. J. & Roth, G. (2006). Acta Cryst. C62, i61-i63.
- Redhammer, G. J., Roth, G. & Amthauer, G. (2006). Acta Cryst. C62, i94-i96.
- Redhammer, G. J., Tippelt, G., Merz, M., Roth, G., Treutmann, W. & Amthauer, G. (2005). Acta Cryst. B61, 367–380.
- Renner, B. & Lehmann, G. (1986). Z. Kristallogr. 175, 43-59.
- Robinson, K., Gibbs, G. V. & Ribbe, P. H. (1971). Science, 172, 567-570.
- Sauerbrei, E. E., Faggiani, R. & Calvo, C. (1973). Acta Cryst. B29, 2304–2306.
- Sheldrick, G. M. (1997). SHELXS97 and SHELXL97. University of Göttingen, Germany.
- Stoe & Cie (1996). X-SHAPE and X-RED. Stoe & Cie, Darmstadt, Germany.
- Tovar, M., Dinnebier, R. E. & Eysel, W. (1998). *Mater. Sci. Forum*, **278**, 750–755.
- Vandenberghe, R. E., Legrand, E., Scheerlinck, D. & Brabers, V. A. M. (1976). Acta Cryst. B32, 2796–2798.